

Reg. No.:	
Name :	

Second Semester B.Sc. Degree (CBCSS – OBE-Regular/Supplementary/ Improvement) Examination, April 2024 (2019 Admission Onwards) CORE COURSE IN PHYSICS 2B02 PHY: Mathematical Physics and Error Analysis

Time: 3 Hours Max. Marks: 40

PART - A

Short answer type. Each carries 1 mark. Answer all questions.

- 1. Define gradient of a scalar function. What is its physical significance?
- 2. What is the resultant of two vectors \vec{A} and \vec{B} acting at an angle θ ?
- 3. What are the limiting values of r, θ , ϕ in spherical polar co-ordinates ?
- 4. Give an example of first order differential equation.
- 5. Explain the uncertainty in q where q = x + y u.
- 6. What are systematic errors?

 $(6 \times 1 = 6)$

PART - B

Short essay questions. Each carries 2 marks. Answer any 6 questions.

- 7. How are the errors propagated in the measurement of difference of two quantities ?
- 8. A student measures the acceleration due to the gravity, five times with the results (all the results in m/s²) 9.9, 9.8, 9.7, 9.6 and 9.5. Find the mean of the readings.
- 9. State the Gauss's divergence theorem.



- 10. Differentiate between irrotational and solenoidal field.
- 11. Show that vectors $\vec{A} = 2\hat{i} 3\hat{j} + 4\hat{k}$ and $\vec{B} = 6\hat{i} + 9\hat{j} 12\hat{k}$ are parallel to each other.
- 12. Solve the equation:

$$\frac{dy}{dx} = \frac{y}{x} + x \sin \frac{y}{x}.$$

- 13. Obtain relations for volume element in curvilinear co-ordinate systems.
- 14. Two resistances $R_1 = (150 \pm 2) \Omega$, $R_2 = (250 \pm 3) \Omega$, are connected in series. What is their equivalent resistance ? (6×2=12)

Short Essay/Problem. Each carries 3 marks. Answer any 4 questions.

- 15. The resultant of two vectors P and Q is R. On reversing the direction of Q, the resultant becomes S. Prove that $R^2 + S^2 = 2(P^2 + Q^2)$.
- 16. Find the gradient of the function $f(x, y, z) = x^2 + y^3 + z^4$.
- 17. Obtain gradient, divergence, curl in curvilinear co-ordinates.
- 18. Solve $(x + 1) \frac{dy}{dx} y = e^x(x + 1)^2$.
- 19. A physical quantity x is given by $x = \frac{a^3b^2}{c\sqrt{d}}$. If the percentage errors of measurement in a, b, c and d are 4%, 2%, 3% and 1% respectively then calculate the percentage error in the calculation of x.
- 20. The length and breadth of a rectangle are (8.7 ± 0.1) cm and (5.4 ± 0.2) cm respectively. Calculate the area and perimeter of the rectangle with error limits. (4×3=12)



PART - D

Long essay type. Each carries 5 marks. Answer any 2 questions.

- 21. Define divergence of a vector field. Mention it geometrical interpretation. If $\vec{A} = 3x^2\hat{i} + 5xy^2\hat{j} + xyz^2\hat{k}$ find ∇ . A at the point (1, 2, 3).
- 22. Define curvilinear coordinates system and derive the expression for gradient operator, divergence, and curl in spherical polar coordinates.
- 23. Let Δx and Δy are the errors associated with variable x and y. Find the propagated error associated with variable z, Δz , for (i) z = ax + by, (ii) z = xy, (iii) z = x/y and (iv) $z = x^c$, where a, b, c are constants.
- 24. Solve $\tan y \frac{dy}{dx} + \tan x = \cos y \cos^2 x$. (2x5=10)

